

On the Direction of Innovation

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Introduction

- Innovation resources unequally distributed across different research areas
- Some areas become more fashionable than others and attract more attention
 - In the 80's leading patent classes in Chemical industry
 - Starting 1995 the areas of computing and electronics surpassed all others by far
- Dot.com bubble is usually viewed as a sign of excessive concentration
- Examples suggest innovation resources might be misallocated across areas
- I examine some possible sources of misallocation

Plan for the Talk

Is there a bias to high return (hot) areas?

Is there a bias towards easy problems?

Rush for the gold?

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Series of Examples

Final unifying framework

Some numerical results

Basic Example

- 2 possible innovations $z_L < z_H$ (cold/hot)
- Social and private value
- 2 innovators
- One time assignment (L,H), (H,H)
- Probabilities: p with one and $q > p$ with two

Is there a bias to hot areas?

Assignment	p_L	p_H	Profits 1	Profits 2	total value
(L,H)	p	p	$p z_L$	$p z_H$	$p(z_L + z_H)$
(H,H)	0	q	$q z_H / 2$	$q z_H / 2$	$q z_H$
Difference			$\Delta \pi_1 = q z_H / 2 - p z_L$	$\Delta \pi_2 = q z_H / 2 - p z_H$	$\Delta V = q z_H - p(z_L + z_H)$

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- It is optimal to have both in H when $\Delta V > 0$

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- It is optimal to have both in H when $\Delta V > 0$
- The market will have both in H when $\Delta\pi_1 > 0$

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- It is optimal to have both in H when $\Delta V > 0$
- The market will have both in H when $\Delta\pi_1 > 0$
- Whenever $\Delta V > 0$, then $\Delta\pi_1 > 0$
- If $q - p < p$ (decreasing returns/duplication/congestion/crowding out):
 - $\Delta\pi_2 < 0$ (pecuniary externality)

Is there a bias to hot areas?

$$z_H = 30, z_L = 16$$

$$p = 1/2, q = 2/3$$

Assignment	p_L	p_H	Profits 1	Profits 2	total value
(L,H)	1/2	1/2	8	15	23
(H,H)	0	2/3	10	10	20
Difference			2	-5	-3

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- When innovator moves from L to H
 - Gets 2 extra (10-8)
 - Other innovator's value decreases by 5 (15-10)
 - Total value falls by 3
- Pecuniary externality

Can the opposite happen?

- 4 innovators
- Probabilities: $p_1 = 1/2$, $p_2 = 3/4$, $p_3 = 1$
- Assignments to consider:
 - 2 in each (LL,HH)
 - 1 in L and 3 in H (L,HHH)

Too Conservative?

Assignment	p_L	p_H	Profits in L	Profits in H	total value
(LL,HH)	3/4	3/4			
(L,HHH)					
Difference					

Too Conservative?

Assignment	p_L	p_H	Profits in L	Profits in H	total value
(LL,HH)	$3/4$	$3/4$	$\frac{3}{8}z_L$	$\frac{3}{8}z_H$	$\frac{3}{8}(z_L + z_H)$
(L,HHH)					
Difference					

Too Conservative?

Assignment	p_L	p_H	Profits in L	Profits in H	total value
(LL,HH)	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{8}z_L$	$\frac{3}{8}z_H$	$\frac{3}{8}(z_L + z_H)$
(L,HHH)	$\frac{1}{2}$	1			
Difference					

Too Conservative?

Assignment	p_L	p_H	Profits in L	Profits in H	total value
(LL,HH)	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{8}z_L$	$\frac{3}{8}z_H$	$\frac{3}{8}(z_L + z_H)$
(L,HHH)	$\frac{1}{2}$	1	$\frac{1}{2}z_L$	$\frac{1}{3}z_H$	$\frac{1}{2}z_L + z_H$
Difference					

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Assignment	p_L	p_H	Profits in L	Profits in H	total value
(LL,HH)	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{8}z_L$	$\frac{3}{8}z_H$	$\frac{3}{8}(z_L + z_H)$
(L,HHH)	$\frac{1}{2}$	1	$\frac{1}{2}z_L$	$\frac{1}{3}z_H$	$\frac{1}{2}z_L + z_H$
Difference			$\frac{1}{8}z_L$		

Too Conservative?

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(LL,HH)	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{8}z_L$	$\frac{3}{8}z_H$	$\frac{3}{8}(z_L + z_H)$
(L,HHH)	$\frac{1}{2}$	1	$\frac{1}{2}z_L$	$\frac{1}{3}z_H$	$\frac{1}{2}z_L + z_H$
Difference			$\frac{1}{8}z_L$	$-2 \times \frac{1}{24}z_H$	

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(LL,HH)	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{8}z_L$	$\frac{3}{8}z_H$	$\frac{3}{8}(z_L + z_H)$
(L,HHH)	$\frac{1}{2}$	1	$\frac{1}{2}z_L$	$\frac{1}{3}z_H$	$\frac{1}{2}z_L + z_H$
Difference			$\frac{1}{8}z_L$	$-2 \times \frac{1}{24}z_H$	$\frac{1}{4}(z_H - z_L)$

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Assignment	p_L	p_H	Profits in L	Profits in H	total value
(LL,HH)	$3/4$	$3/4$	$\frac{3}{8}z_L$	$\frac{3}{8}z_H$	$\frac{3}{4}(z_L + z_H)$
(L,HHH)	$1/2$	1	$\frac{1}{2}z_L$	$\frac{1}{3}z_H$	$\frac{1}{2}z_L + z_H$
Difference			$\frac{1}{8}z_L$	$-2 \times \frac{1}{24}z_H$	$\frac{1}{4}(z_H - z_L)$

- (L, HHH) maximizes total value

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(L,HHH)	1/2	1	$\frac{1}{2}z_L$	$\frac{1}{3}z_H$	$\frac{1}{2}z_L + z_H$
Difference			$\frac{1}{8}z_L$	$-2 \times \frac{1}{24}z_H$	$\frac{1}{4}(z_H - z_L)$

- (L, HHH) maximizes total value
- Changes in profits for mover: $\frac{1}{3}z_H - \frac{3}{8}z_L$
 - Negative if z_L is close to z_H

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(LL,HH)	$3/4$	$3/4$	$\frac{3}{8}z_L$	$\frac{3}{8}z_H$	$\frac{3}{4}(z_L + z_H)$
(L,HHH)	$1/2$	1	$\frac{1}{2}z_L$	$\frac{1}{3}z_H$	$\frac{1}{2}z_L + z_H$
Difference			$\frac{1}{8}z_L$	$-2 \times \frac{1}{24}z_H$	$\frac{1}{4}(z_H - z_L)$

- (L, HHH) maximizes total value
- Changes in profits for mover: $\frac{1}{3}z_H - \frac{3}{8}z_L$
 - Negative if z_L is close to z_H
- Pecuniary externalities: $\frac{1}{8}z_L - \frac{1}{12}z_H$

General Insight

- Market will in general assign innovation resources inefficiently
- Pecuniary external effect from congestion/crowding out
 - Differential rent dissipation/value burning with congestion
- Bias depends on relative size of pecuniary effects
- If stronger in more crowded areas then bias to hot areas.
- Depends on $P(m)$. Satisfied in standard cases.

Go for the Low Hanging Fruit?

- 2 innovators
- 2 Innovations (L, H) and $z_L = z_H = z$
- Probabilities: $p_L = (0.9, 1)$, $p_H = (1/5, 1/3)$

Bias to the low hanging fruit

Assignment	p_L	p_H	Profits		total value
			Innovator 1	Innovator 2	
(H,L)	0.9	0.2	$0.2z$	$0.9z$	$1.1z$
(L,L)	1	0	$0.5z$	$0.5z$	z
			$0.3z$	$-0.4z$	$-0.1z$

Bias to the low hanging fruit

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(H,L)	0.9	0.2	$0.2z$	$0.9z$	$1.1z$
(L,L)	1	0	$0.5z$	$0.5z$	z
			$0.3z$	$-0.4z$	$-0.1z$

- Outcome: (L,L)
- Not Efficient
- External effect: $-0.4z$

Rush for the Gold?

- Innovators can be reallocated after discovery
- Cost of switching $c \geq 0$
- Same technology as in our first example: $0 < p < q$
- Eventually both discovered. No discounting
- Alternative allocations:
 - 1 Both innovators on H until discovery then switch to L .
 - 2 One in each. After first discovery both on remaining.

Rush for the Gold?

Initial assign		prob	Payoffs		total value
			Innovator 1 (L)	Innovator 2 (H)	
(L, H)					
(H, H)	Expected payoffs		$\frac{1}{2} (z_H + z_L) - c$	$\frac{1}{2} (z_H + z_L) - c$	$z_H + z_L - 2c$
Difference					

Rush for the Gold?

Initial assign		prob	Payoffs		total value
			Innovator 1 (L)	Innovator 2 (H)	
(L, H)	L discovered first	$1/2$			
(H, H)	Expected payoffs		$\frac{1}{2} (z_H + z_L) - c$	$\frac{1}{2} (z_H + z_L) - c$	$z_H + z_L - 2c$
Difference					

Rush for the Gold?

Initial assign		prob	Payoffs		total value
			Innovator 1 (L)	Innovator 2 (H)	
(L, H)	L discovered first	1/2	$z_L + \frac{1}{2}z_H - c$		
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
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(L, H)	L discovered first	$1/2$	$z_L + \frac{1}{2}z_H - c$	$\frac{1}{2}z_H$	
	H discovered first	$1/2$			
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
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(L, H)	L discovered first	$1/2$	$z_L + \frac{1}{2}z_H - c$	$\frac{1}{2}z_H$	
	H discovered first	$1/2$	$z_L/2$		
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
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	Expected payoffs				
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
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	H discovered first	1/2	$z_L/2$	$z_H + \frac{1}{2}z_L - c$	
	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$		
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
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	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
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	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	$z_H + z_L - c$
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	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	$z_H + z_L - c$
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Difference			$\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$		

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	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	$z_H + z_L - c$
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
Difference			$\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	

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	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	$z_H + z_L - c$
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
Difference			$\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-c$

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	H discovered first	1/2	$z_L/2$	$z_H + \frac{1}{2}z_L - c$	
	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	$z_H + z_L - c$
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	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	$z_H + z_L - c$
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Difference			$\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-c$

- Socially inefficient to rush for the gold

Rush for the Gold?

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	H discovered first	1/2	$z_L/2$	$z_H + \frac{1}{2}z_L - c$	
	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	$z_H + z_L - c$
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Difference			$\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-c$

- Socially inefficient to rush for the gold
- The market will rush for the gold if $c < \frac{1}{2}(z_H - z_L)$

Rush for the Gold?

Initial assign		prob	Payoffs		total value
			Innovator 1 (L)	Innovator 2 (H)	
(L, H)	L discovered first	1/2	$z_L + \frac{1}{2}z_H - c$	$\frac{1}{2}z_H$	
	H discovered first	1/2	$z_L/2$	$z_H + \frac{1}{2}z_L - c$	
	Expected payoffs		$\frac{3}{4}z_L + \frac{1}{4}z_H - \frac{1}{2}c$	$\frac{3}{4}z_H + \frac{1}{4}z_L - \frac{1}{2}c$	$z_H + z_L - c$
(H, H)	Expected payoffs		$\frac{1}{2}(z_H + z_L) - c$	$\frac{1}{2}(z_H + z_L) - c$	$z_H + z_L - 2c$
Difference			$\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$	$-c$

- Socially inefficient to rush for the gold
- The market will rush for the gold if $c < \frac{1}{2}(z_H - z_L)$
- Pecuniary externality: $-\frac{1}{4}(z_H - z_L) - \frac{1}{2}c$
- Similar effects for low hanging fruit

Summary External Effects

Source	Direction of Bias	
	High and low z	Different p 's
Congestion/market stealing	Could go either way	Low hanging fruit
	Under usual assumptions to hot areas	
Duplication cost externalities	Hot areas	Low hanging fruit
Returns on future innovations	Hot areas	Low hanging fruit

General Dynamic Model

- Values: $z_1 \leq z_2, \dots, \leq z_N$
- Assignment $m(z)$
- Continuous arrival of new problems $F(z)$
- Probability of innovation with m innovators: $P(m(z)) = \exp(-\lambda m)$
- Flow λM exit of solved problems
- All above some threshold z_0
- Compare Market vs Efficient assignment

Market vs Efficient

	Market	Efficient
Assignment	Excessive concentration in hot areas	More balanced assignment
Opportunities available	Less attractive alternatives left	More attractive alternatives left
Turnover of innovators	Excessively high	More moderate
Flow of Value	$\lambda M z_0$	$\lambda ME(z z \geq z_0) - D(c)$
Efficient/Market value	over 3.5 for $c = 1$ million	
	close to 6 as $c \rightarrow 0$	

Final Remarks

- Market can misallocate innovation resources
- Found new sources of market failure:
 - Congestion
 - Excess turnover
 - Run for the gold
- The costs can be large
- Source of Market Failure: Lack of property rights over “problems”
- Patents do not address this sort of market failure